

7.  $P = ((\text{NOT } A) \text{ OR } B) \text{ AND } C$

8.  $P = \text{NOT}((\text{NOT } A) \text{ AND } B)$

9.  $P = (A \text{ OR } B) \text{ AND } (C \text{ OR } D)$

10.  $P = \text{NOT}((A \text{ OR } B) \text{ AND } C)$

11.  $P = A \text{ OR } B \text{ OR } C \text{ OR } D$

12.  $P = (A \text{ AND } B) \text{ AND } \text{NOT } C$

# Binary Logic

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Your name:
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## Activity 1: How many values?

How many different ways can we arrange four bits in one nibble?

0	0	0	0
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1	1	1	1
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## Activity 2: Representing small numbers in binary

The denary number 13 in binary is written 1101

$$13 = \begin{array}{|c|c|c|c|} \hline 8 & 4 & 2 & 1 \\ \hline 1 & 1 & 0 & 1 \\ \hline \end{array} = 1101$$

Use the place value tables below to write the following numbers in binary.

$$9 = \begin{array}{|c|c|c|c|} \hline 8 & 4 & 2 & 1 \\ \hline & & & \\ \hline \end{array} = \underline{\hspace{2cm}}$$

$$14 = \begin{array}{|c|c|c|c|} \hline 8 & 4 & 2 & 1 \\ \hline & & & \\ \hline \end{array} = \underline{\hspace{2cm}}$$

Without place value tables:

$$11 = \underline{\hspace{2cm}} \qquad 7 = \underline{\hspace{2cm}}$$

$$5 = \underline{\hspace{2cm}} \qquad 8 = \underline{\hspace{2cm}}$$

$$\underline{\hspace{2cm}} = 0110 \qquad \underline{\hspace{2cm}} = 1100$$

What about this one?

$$23 = \underline{\hspace{2cm}}$$

## Activity 7 Logic Charts

Draw logic charts for the following logic statements. You will need to use a maximum of three logic gates (OR, AND, NOT) for each question.

1.  $P = \text{NOT } A$

2.  $P = A \text{ AND } B$

3.  $P = A \text{ OR } B$

4.  $P = \text{NOT } (A \text{ AND } B)$

5.  $P = (A \text{ AND } B) \text{ OR } C$

6.  $P = \text{NOT } (A \text{ OR } B) \text{ AND } C$

# Nightclub Doorman Checks Activity 6

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You have been asked by “the management” of Horbury Gardens to write a set of rules that must be checked when the doormen are letting customers into the nightclub.

**1. Write some rules that the customers must have when they come in**

a. Rule 1 \_\_\_\_\_

b. Rule 2 \_\_\_\_\_

c. Rule 3 \_\_\_\_\_

**2. There are two ways in which customers could still be allowed into the nightclub even if they didn't follow the rules. What are they?**

a. Exception 1 \_\_\_\_\_

b. Exception 2 \_\_\_\_\_

If two rules both HAVE to be followed, we can add them together for example at Horbury Academy, you need your planner AND your five a day.

Sometimes we can make exceptions, for example you must have your tie on OR a uniform note in your planner.

Using the words “AND” and “OR”, can you group the nightclub rules together to make one single rule that the bouncers could use?

### Activity 3: Representing larger numbers in binary

Each individual digit in a binary number is a binary digit or “bit” for short. A bit can only have the values 0 or 1.

Usually bits are grouped by eight, and called a “byte”. When we represent numbers in binary we shall usually use whole bytes.

Fill in this place value table, with the place values for 8 bits.


Use these place values to do the following conversions between binary and denary.

$$47 = \begin{array}{|c|c|c|c|c|c|c|c|} \hline & & & & & & & & \\ \hline & & & & & & & & \\ \hline \end{array} = \underline{\hspace{2cm}}$$

$$\underline{\hspace{2cm}} = \begin{array}{|c|c|c|c|c|c|c|c|} \hline & & & & & & & & \\ \hline & & & & & & & & \\ \hline \end{array} = 01100100$$

Try these without the place value table.

Denary → Binary

Denary ← Binary

$$135 = \underline{\hspace{2cm}} \qquad \underline{\hspace{2cm}} = 10000011$$

$$73 = \underline{\hspace{2cm}} \qquad \underline{\hspace{2cm}} = 01010111$$

$$245 = \underline{\hspace{2cm}} \qquad \underline{\hspace{2cm}} = 11100101$$

What are the largest and smallest numbers you can represent in a byte?

To make a byte easier to read, it is usually divided into groups of 4, called nibbles e.g. 1110 0101.

What is the meaning of the following terms?

- kilobyte (kB)
- megabyte (MB)
- gigabyte (GB)
- terabyte (TB)

## Activity 4: Adding binary numbers

We can add binary numbers by columns.

If the total for a column is two (in binary 10) we write down 0 and “carry 1” to the next column.

If the total for a column is three (in binary, 11) we write down 1 and carry 1.

Try these:

$$\begin{array}{rcccccccc} & 1 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & (169) \\ + & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & (42) \\ \hline \end{array}$$

$$\begin{array}{rcccccccc} & 0 & 1 & 0 & 1 & 1 & 0 & 1 & 1 & (91) \\ + & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 1 & (57) \\ \hline \end{array}$$

What about this one?

$$\begin{array}{rcccccccc} & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 0 \\ + & 0 & 0 & 1 & 1 & 0 & 0 & 1 & 1 \\ \hline \end{array}$$

This is a special case which results in an “overflow”, which is technically an error when we use eight bit bytes.

## Activity 5 Binary Logic

	1	1	0	1	1	0	1	0
AND	0	0	1	1	0	0	1	1

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	1	1	0	1	1	0	1	0
OR	0	0	1	1	0	0	1	1

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	1	1	0	0	1	1	1	0
AND	1	0	0	1	0	1	1	1

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	1	1	0	0	1	1	1	0
OR	1	0	0	1	0	1	1	1

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	1	1	1	1	1	1	1	1
AND	1	0	1	0	1	0	1	0

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	1	1	1	1	1	1	1	1
OR	1	0	1	0	1	0	1	0

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